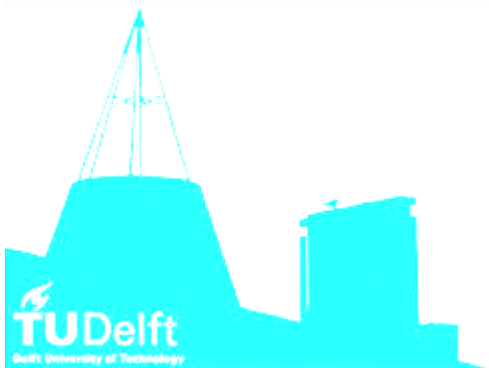




Pengcheng Huang  
Georgia Giannopoulou  
Lothar Thiele

# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores

RTAS 2016



Sujay Narayana  
R. Venkatesha Prasad

Why?

# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores

Why?

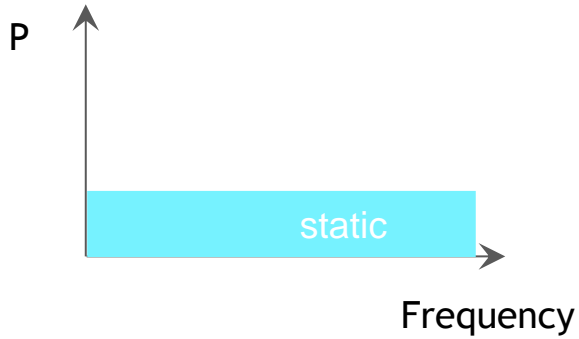
Embedded system industry is moving towards MC, but little has been done on

“Exploring Energy Saving for  
Mixed-Criticality Systems on Multi-cores”

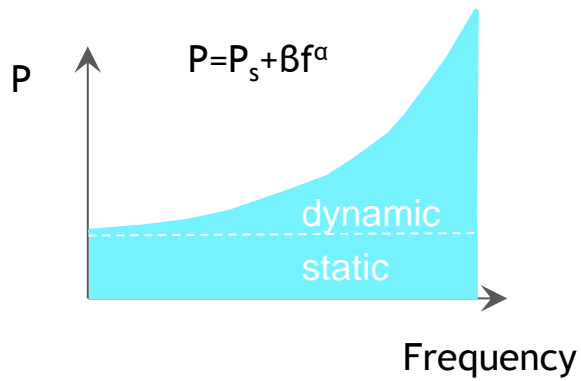
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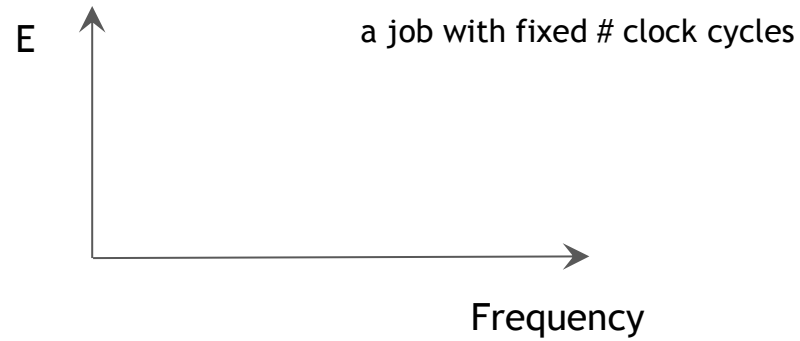
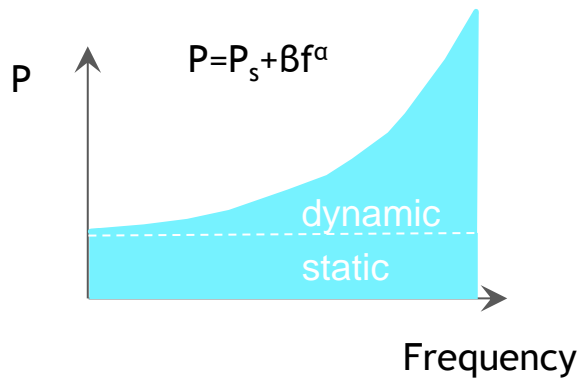
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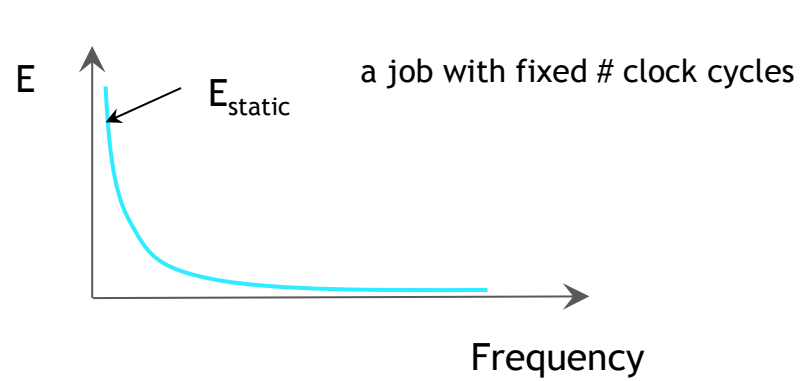
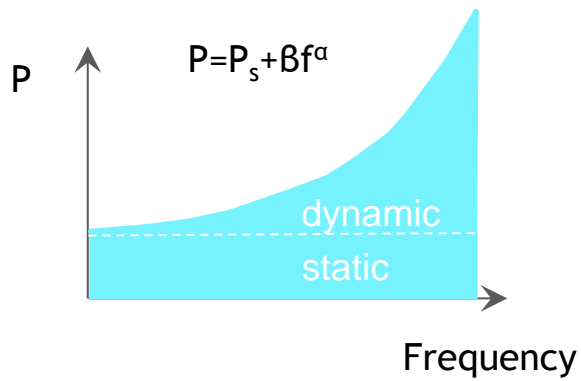


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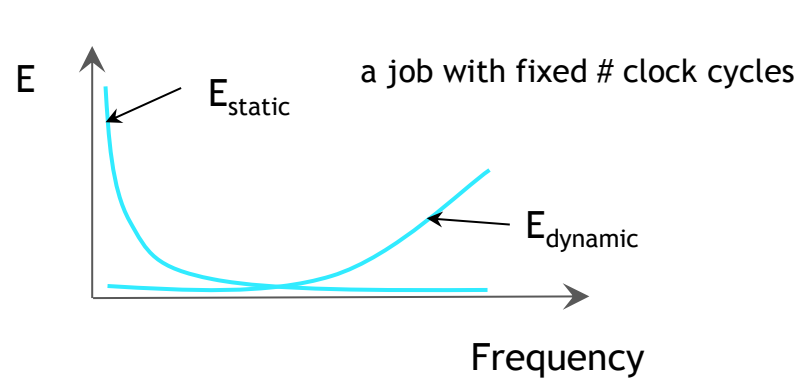
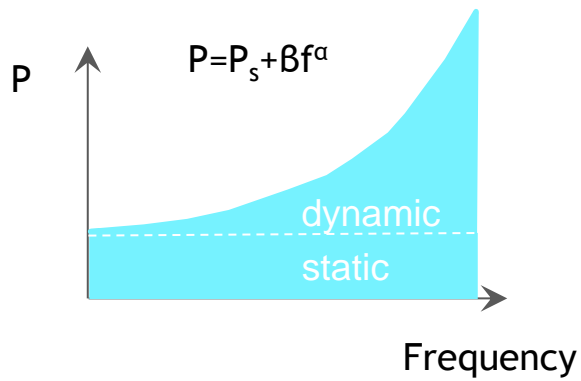


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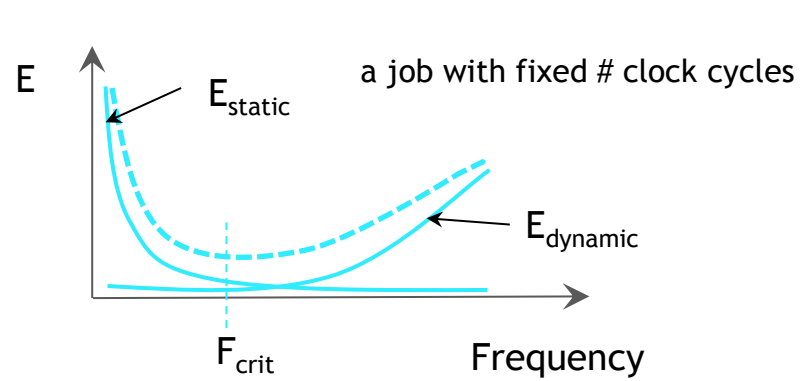
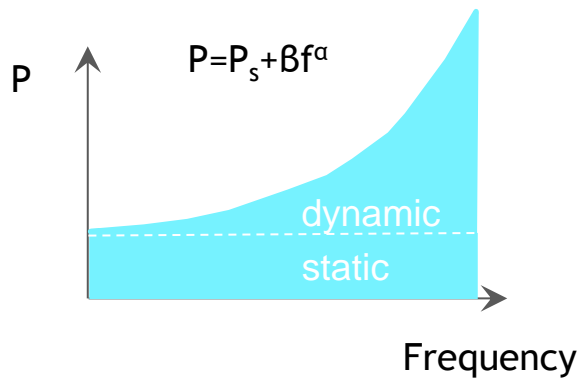




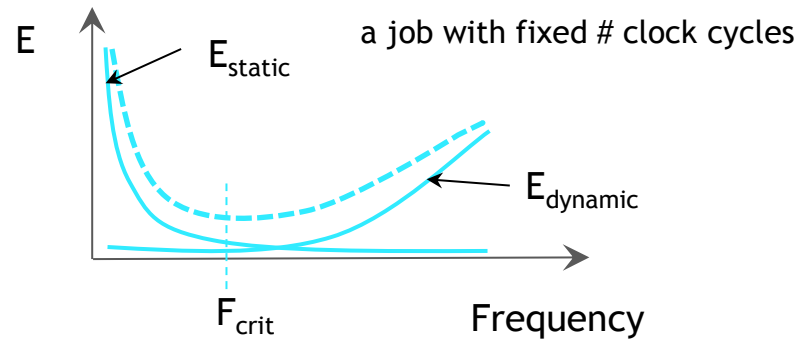
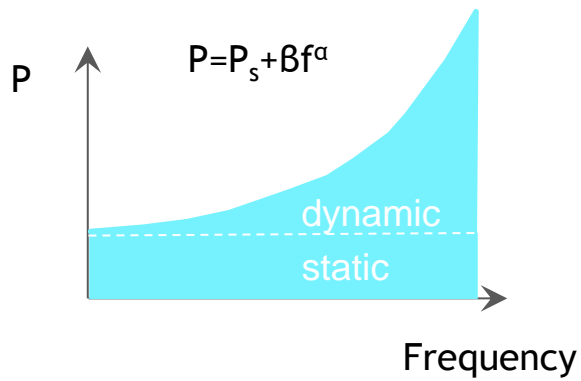
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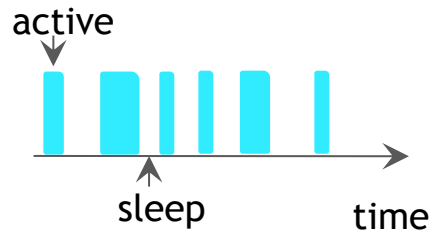
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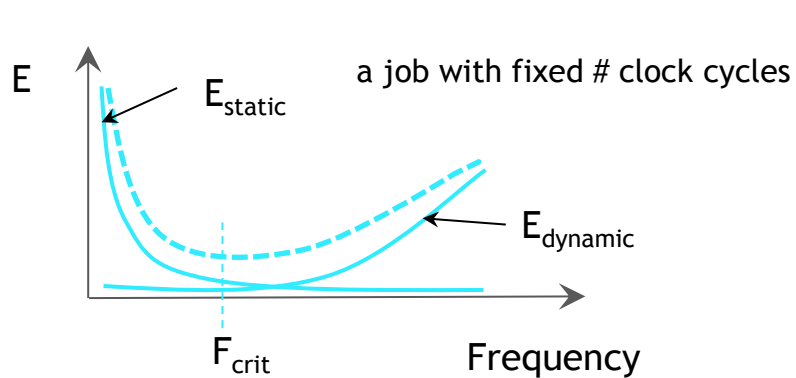
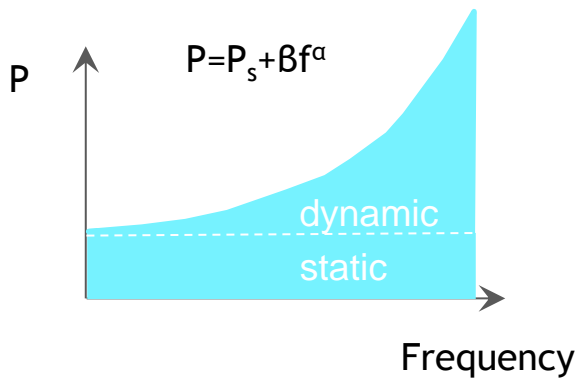


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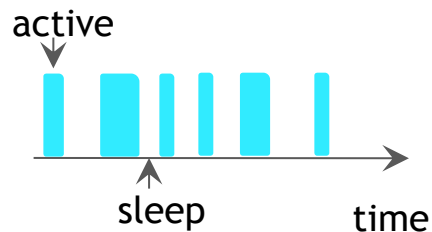


# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores





# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores



DVFS, frequency  $\geq F_{\text{crit}}$   
 no energy dissipation when sleep  
 zero overhead sleep  $\leftrightarrow$  active

find frequencies  $\rightarrow$  minimize energy  
 well studied problem for classical systems

# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores

apps of varying criticality levels

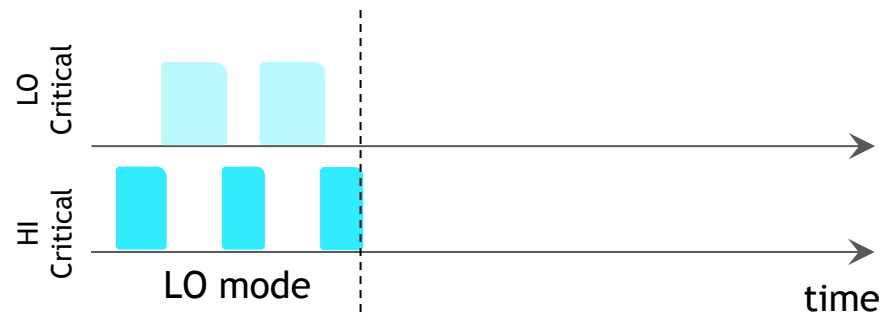
share a common platform

time overrun is a concern

asymmetric isolation

# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores

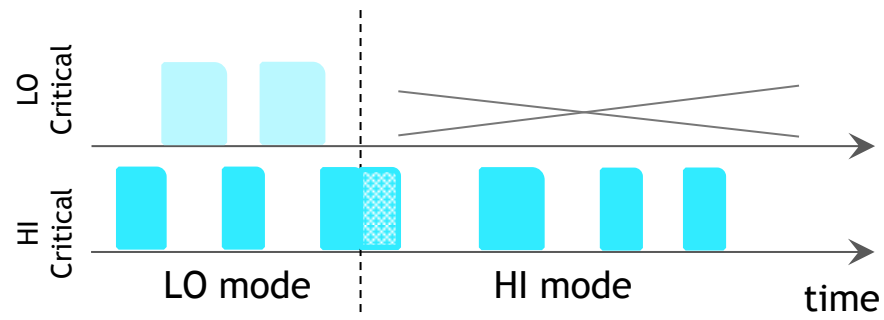
- apps of varying criticality levels
- share a common platform
- time overrun is a concern
- asymmetric isolation



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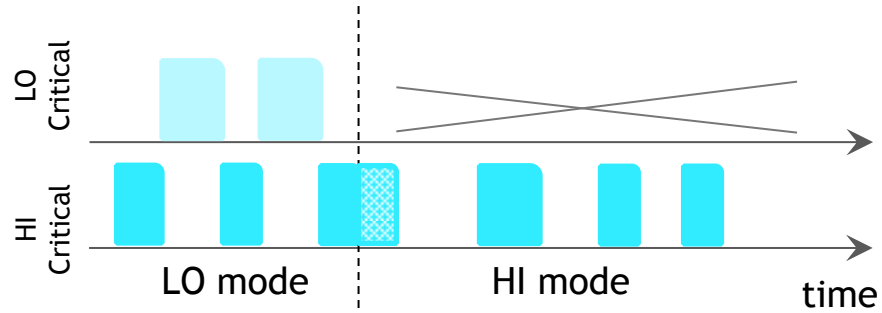
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# Exploring Energy Saving for Mixed-Criticality Systems on Multi-cores

apps of varying criticality levels  
share a common platform  
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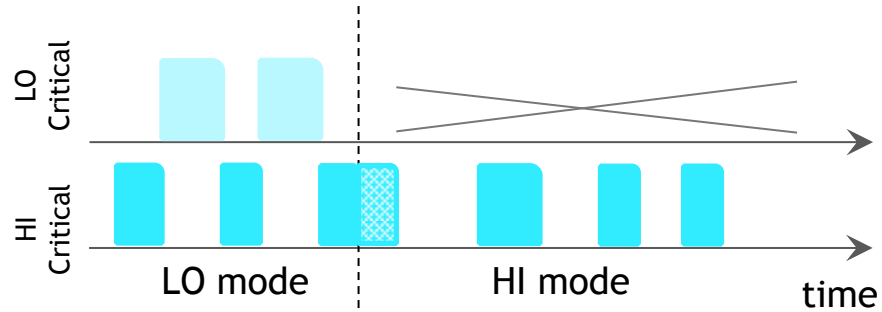
EDF-VD for sporadic tasks  
( $T_i$ ,  $D_i$ ,  $C_i(\text{LO})$ ,  $C_i(\text{HI})$ )

Safety preparation

HI tasks' deadlines shortened  
by a factor  $x < 1$  in LO mode

apps of varying criticality levels  
share a common platform  
time overrun is a concern

asymmetric isolation

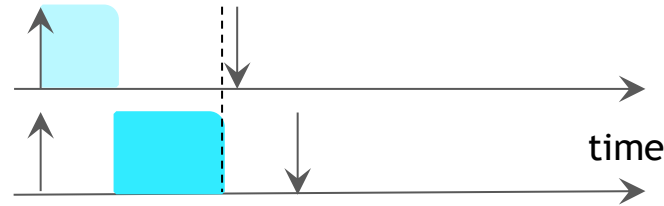


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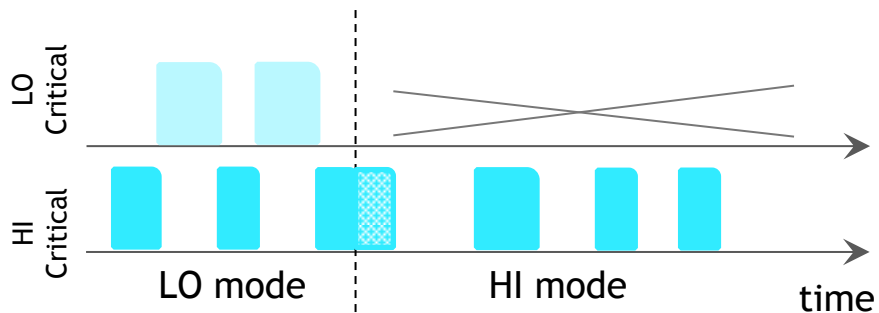
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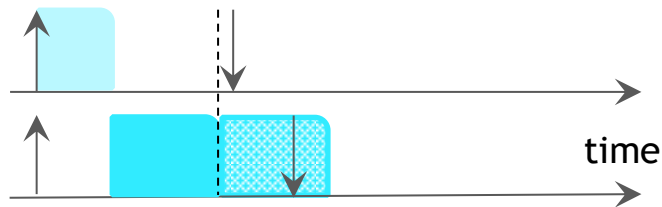


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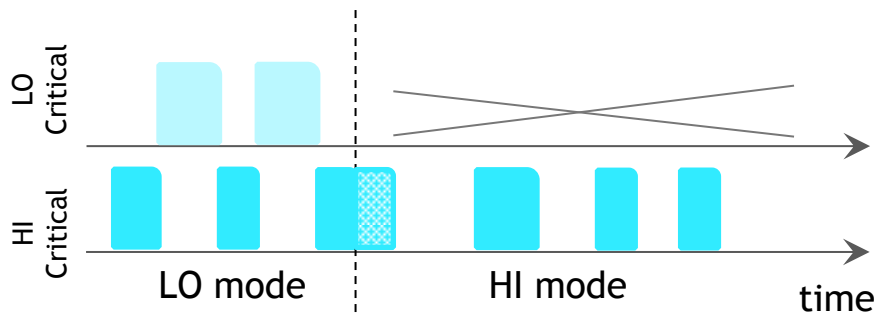
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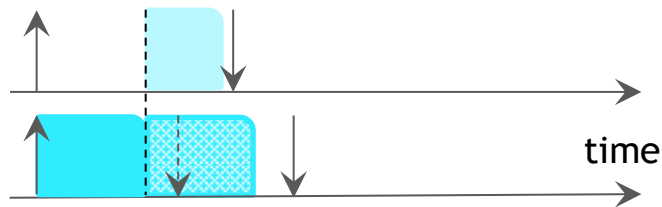


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EDF-VD for sporadic tasks  
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Safety preparation

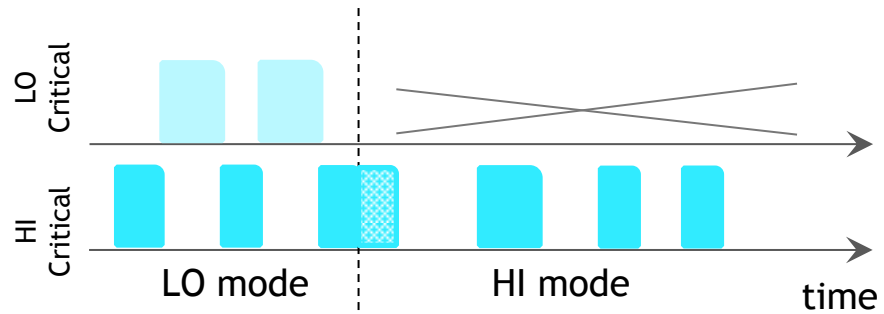
HI tasks' deadlines shortened  
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Is it fundamentally different?

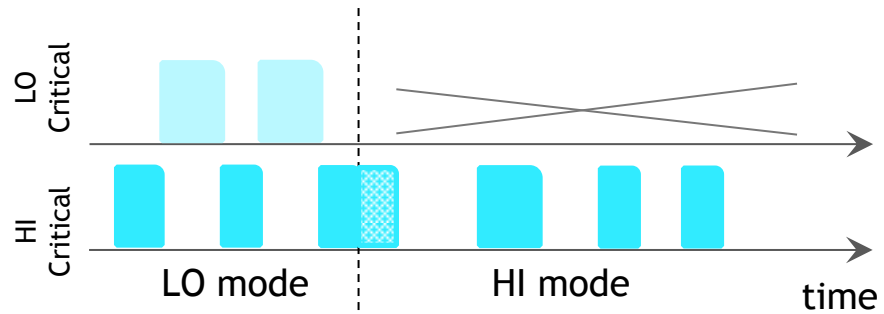
Let us focus on unicore first.

## Intrinsically Dynamic



1. For which mode(s) should we minimize energy consumption?
2. Relation between LO and HI mode minimal energy consumptions?
3. Impact of safety preparation?

## Intrinsically Dynamic

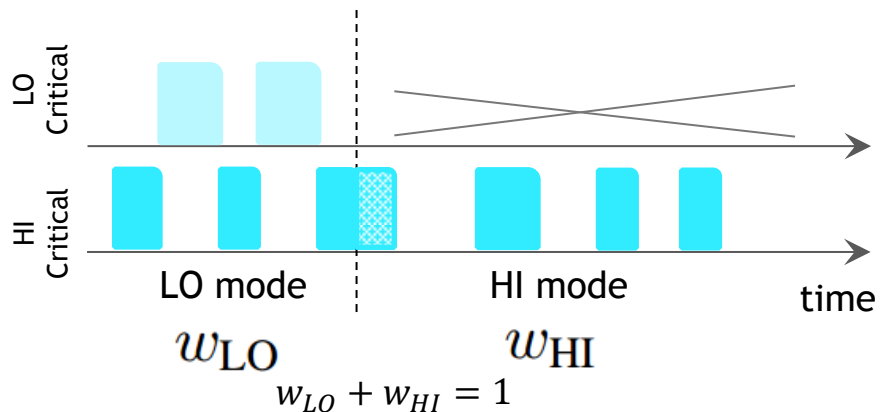


1. For which mode(s) should we minimize energy consumption?

- HI mode is unlikely, hence focus on LO mode<sup>+</sup>.
- HI mode probability increases with time, minimize both.



## Intrinsically Dynamic



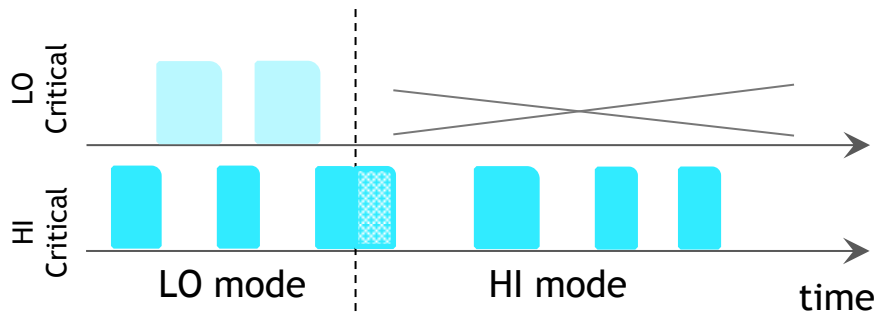
Minimize a weighted sum of energy dissipations in both modes.

$$E_{LO} = w_{LO} \sum_{\tau_i \in \tau} \frac{C_i(\text{LO})}{T_i} \frac{f_b}{f_i^{\text{LO}}} (P_s + \beta (f_i^{\text{LO}})^\alpha)$$

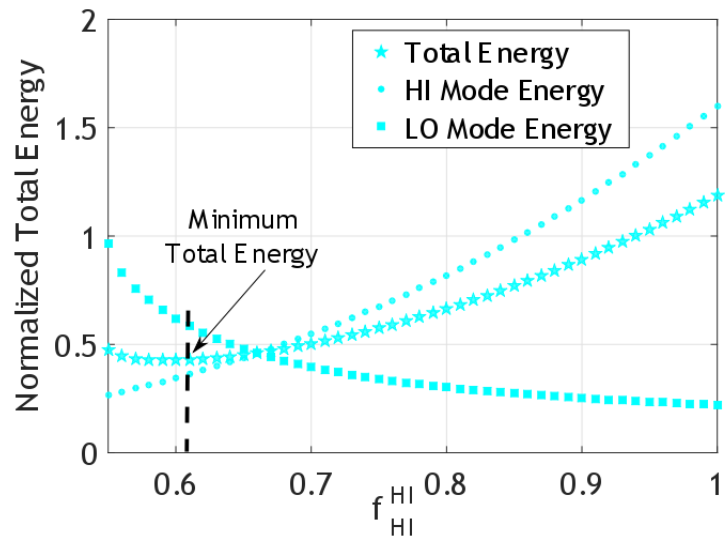
$$E_{HI} = w_{HI} \sum_{\tau_i \in \tau_{HI}} \frac{C_i(\text{HI})}{T_i} \frac{f_b}{f_i^{\text{HI}}} (P_s + \beta (f_i^{\text{HI}})^\alpha).$$

$$E = E_{LO} + E_{HI}$$

# Intrinsically Dynamic



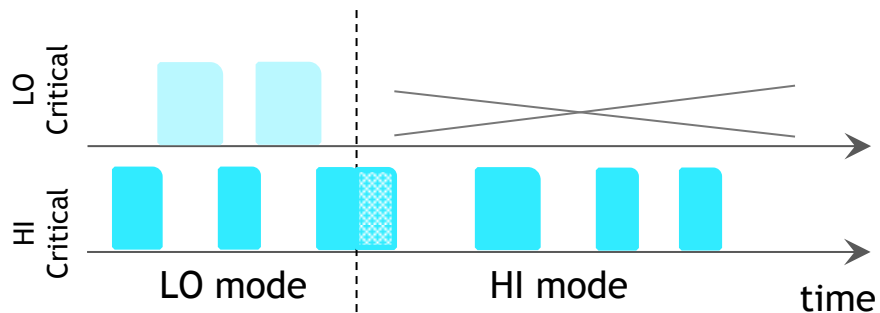
## 2. Relation between LO and HI mode minimal energy consumptions?



$$w_{HI} = 0.65$$

Example task set  
3 HI, 2 LO

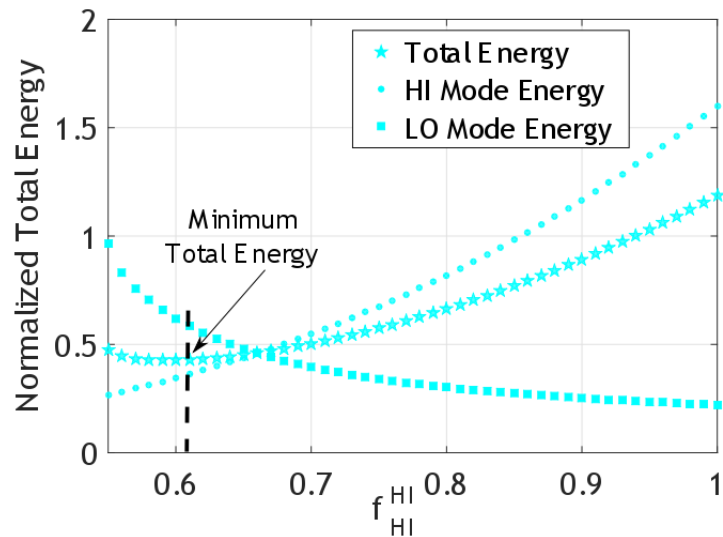
## Intrinsically Dynamic



## 2. Relation between LO and HI mode minimal energy consumptions?

Speedup in HI mode  $\rightarrow$  Less pressure in LO mode

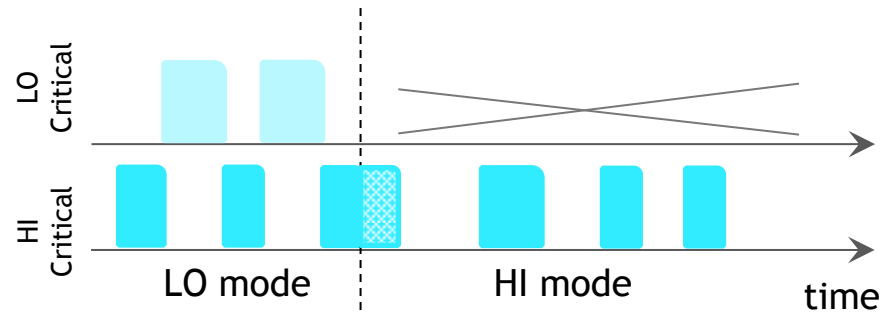
Higher HI energy  $\rightarrow$  Lower LO energy



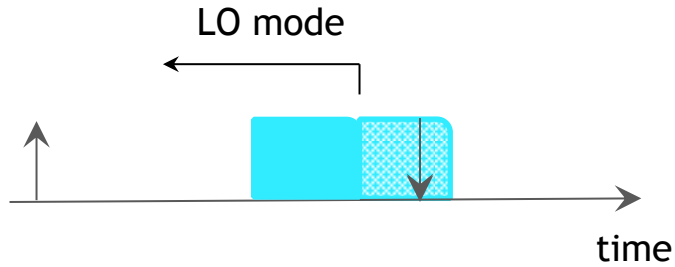
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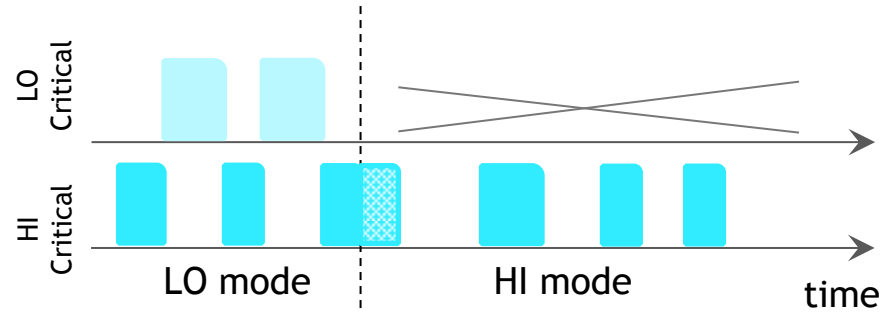
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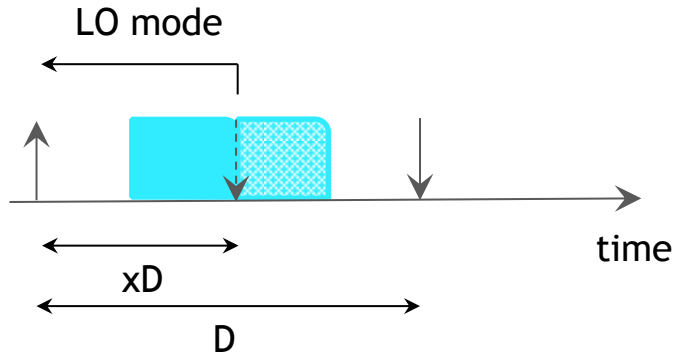
## 3. Impact of safety preparation?



# Intrinsically Dynamic



## 3. Impact of safety preparation?



More preparation →

Load shifted more to LO mode →

Higher LO mode energy &  
Lower HI mode energy

Knowing the characteristics,

how can we solve the unicorn problem algorithmically?

## The “easy” way

$$\begin{array}{ll} \text{minimize} & E = E_{\text{LO}} + E_{\text{HI}} \\ \text{s.t.} & \frac{\tilde{U}_{\text{HI}}^{\text{LO}}}{x} + \tilde{U}_{\text{LO}}^{\text{LO}} \leq 1 \\ & x\tilde{U}_{\text{LO}}^{\text{LO}} + \tilde{U}_{\text{HI}}^{\text{HI}} \leq 1 \\ & x \in [\hat{x}_{\text{LB}}, \hat{x}_{\text{UB}}] \\ & \forall \tau_i, \forall \chi, f_i^X \in [f_{\text{min}}, f_{\text{max}}] \end{array}$$

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It's a convex programming problem!

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Even “better”, one can apply KKT conditions!

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Even “better”, one can apply KKT conditions!

Lagrange multiplier method  
extended for inequality

Is that all for unicorn?

What are good insights leading to a faster algorithmic solution?

## Reduce frequency search space

$$\underline{\forall \tau_i \in \tau_{\text{LO}}, f_i^{\text{LO}} = f_{\text{LO}}^{\text{LO}}; \quad \forall \tau_i \in \tau_{\text{HI}}, f_i^{\text{LO}} = f_{\text{HI}}^{\text{LO}} \wedge f_i^{\text{HI}} = f_{\text{HI}}^{\text{HI}}.}$$

## Reduce frequency search space

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**consider**  $\tau_i$  and  $\tau_j$

**minimize**

$$E_{\text{HI}} = w_{\text{HI}} \left( u_i \frac{f_b}{f_i^{\text{HI}}} (P_s + \beta (f_i^{\text{HI}})^\alpha) \right) \\ + w_{\text{HI}} \left( u_j \frac{f_b}{f_j^{\text{HI}}} (P_s + \beta (f_j^{\text{HI}})^\alpha) \right)$$

**s.t.**  $u_i \frac{f_b}{f_i^{\text{HI}}} + u_j \frac{f_b}{f_j^{\text{HI}}} \leq u_{i+j}$

## Reduce frequency search space

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## Reduce frequency search space

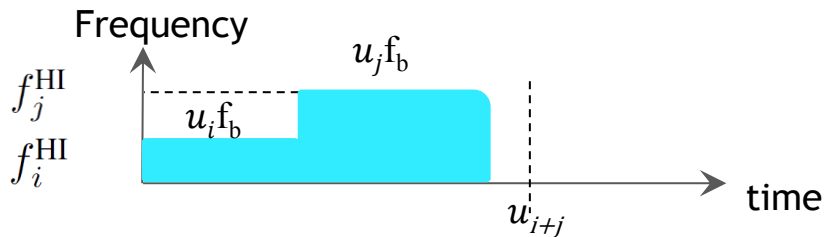
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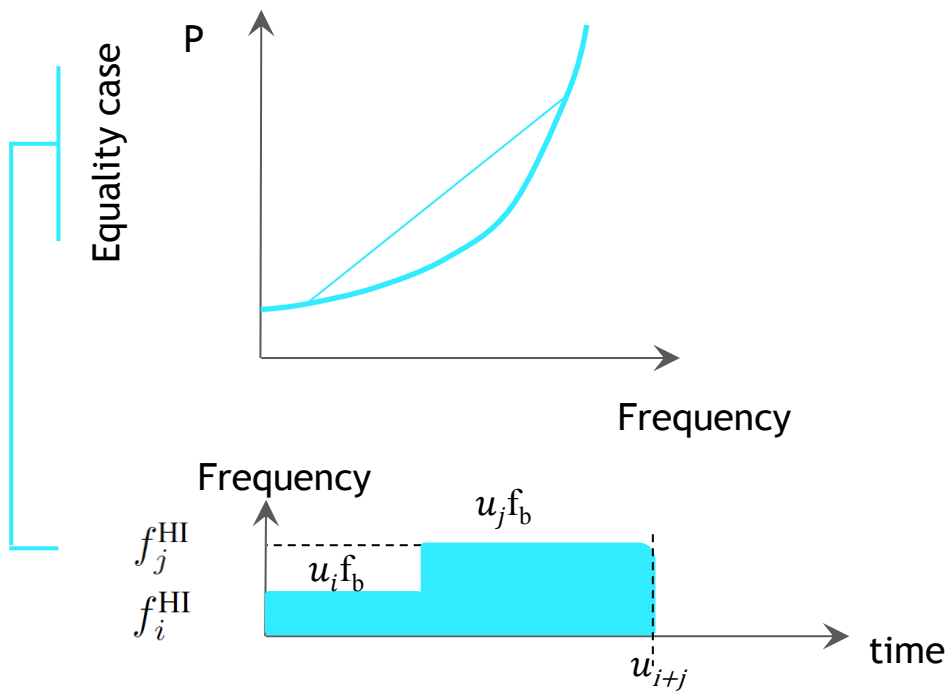




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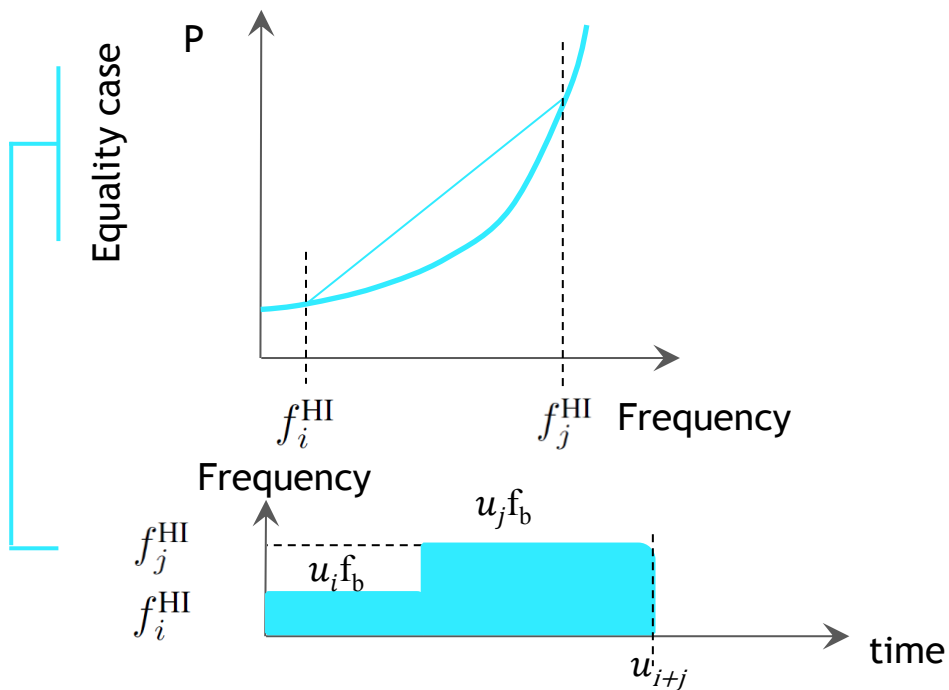
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## Reduce frequency search space

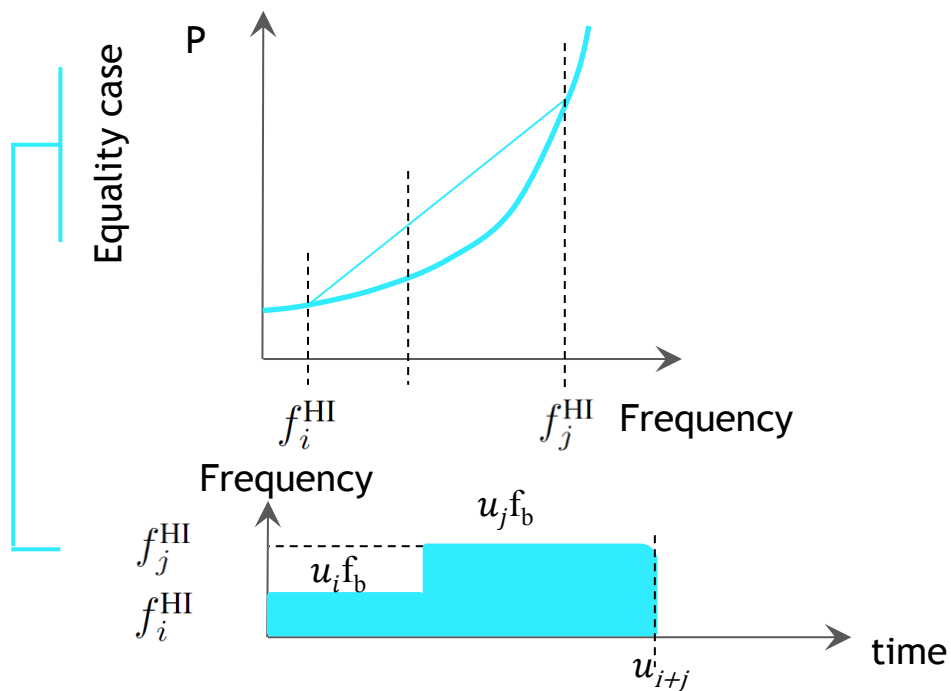
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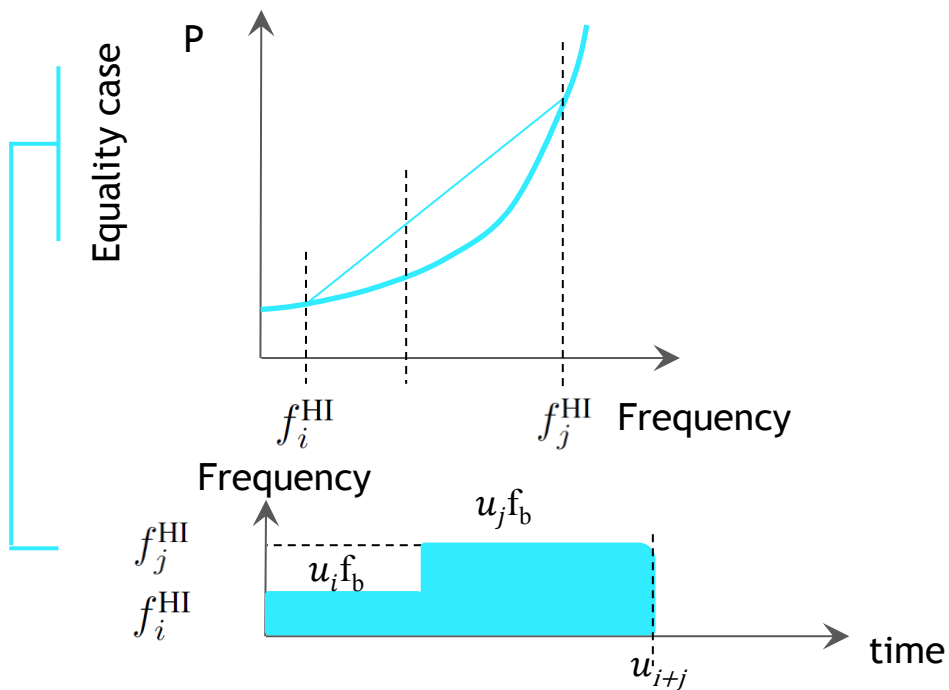
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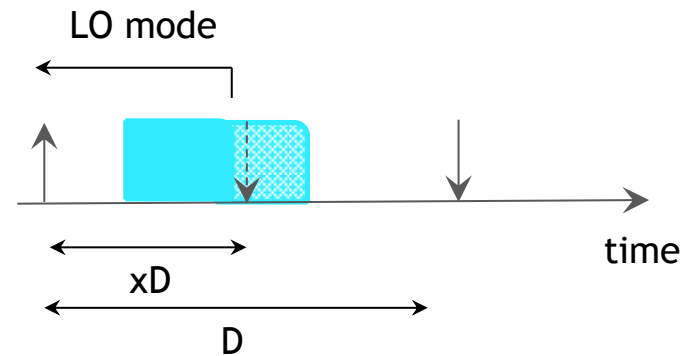
General case proved by KKT

## “Optimal” safety preparation

- 1 Extreme case, i.e.  $f_{LO}^{LO} = f_{HI}^{LO} = f_{HI}^{HI} = f_{\min}$ .
  - 2 Equilibrium case, i.e.  $x_{LBopt} = x_{opt} = x_{UBopt}$ .
-

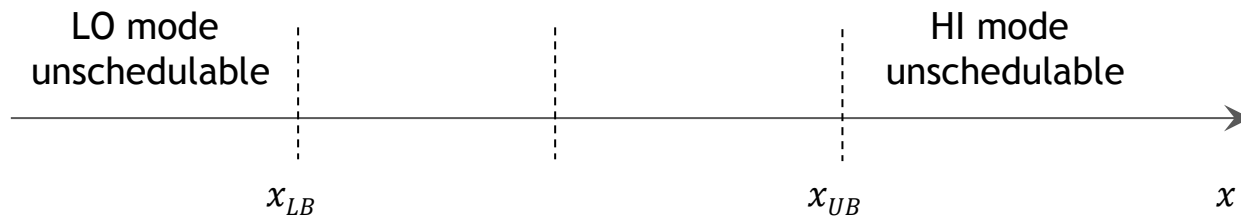
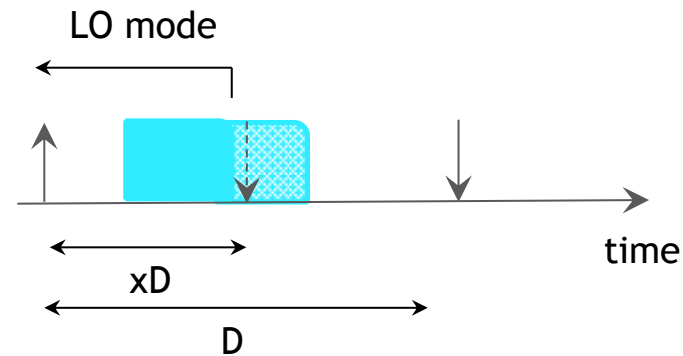
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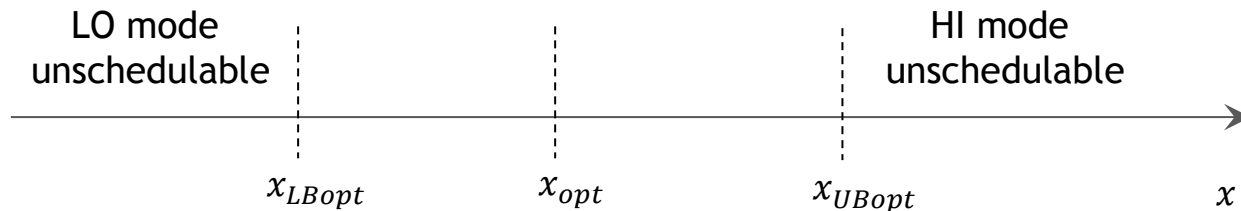
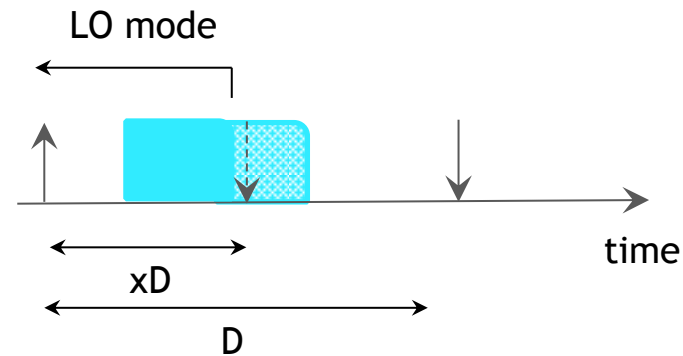
## “Optimal” safety preparation

- 1 Extreme case, i.e.  $f_{LO}^{LO} = f_{HI}^{LO} = f_{HI}^{HI} = f_{\min}$ .
  - 2 Equilibrium case, i.e.  $x_{LBopt} = x_{opt} = x_{UBopt}$ .
- 



## “Optimal” safety preparation

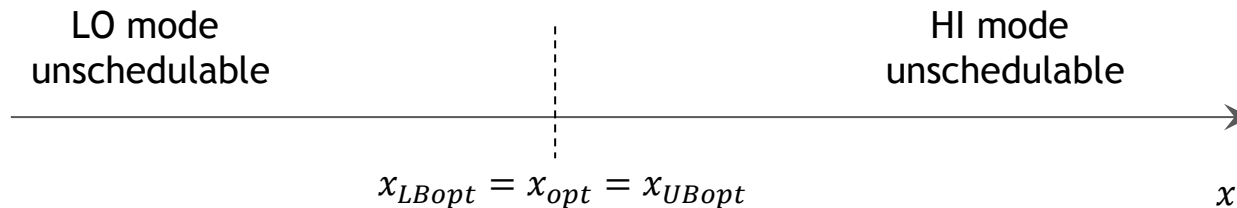
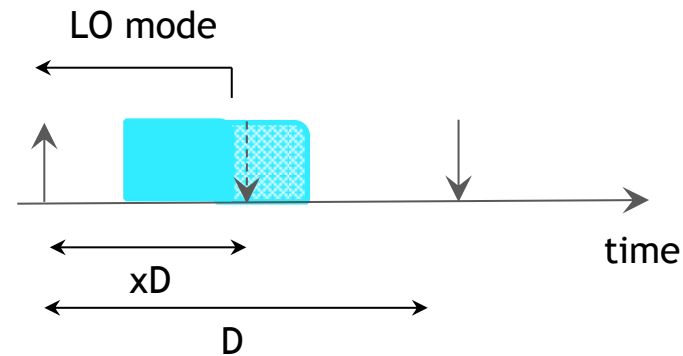
- 1 Extreme case, i.e.  $f_{LO}^{LO} = f_{HI}^{LO} = f_{HI}^{HI} = f_{\min}$ .
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- 





## “Optimal” safety preparation

- 1 Extreme case, i.e.  $f_{LO}^{LO} = f_{HI}^{LO} = f_{HI}^{HI} = f_{\min}$ .
  - 2 Equilibrium case, i.e.  $x_{LBopt} = x_{opt} = x_{UBopt}$ .
- 



Reduce frequency search space

“Optimal” safety preparation



Numerical solution to the optimization problem with logarithmic complexity

Multicore

Let us focus on partitioned scheduling first.

Multicore

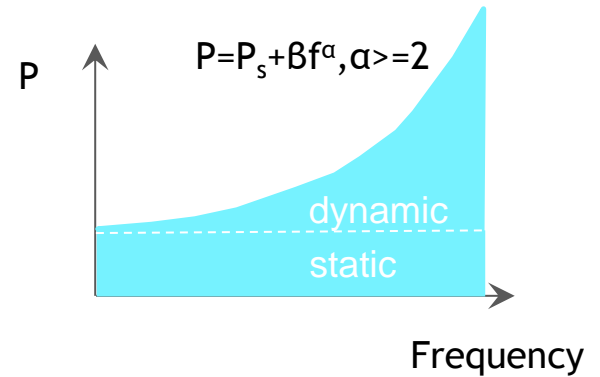
Let us focus on partitioned scheduling first.

We only need to solve the partitioning.

A general intuition

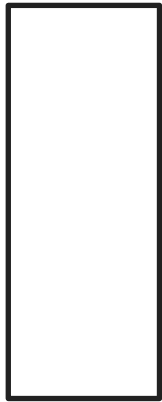
Cores should have equal chances to “relax”.

Energy is saved mostly through the “initial” phase.



How good are existing methods?

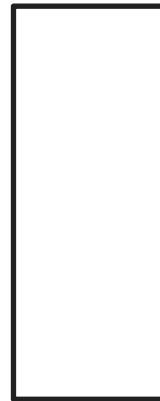
Method 1<sup>+</sup> (M1)



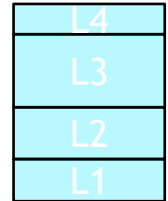
Core1



Core2



Core3



Method 1<sup>+</sup> (M1)



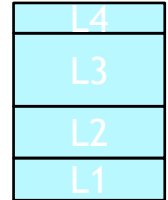
Core1



Core2



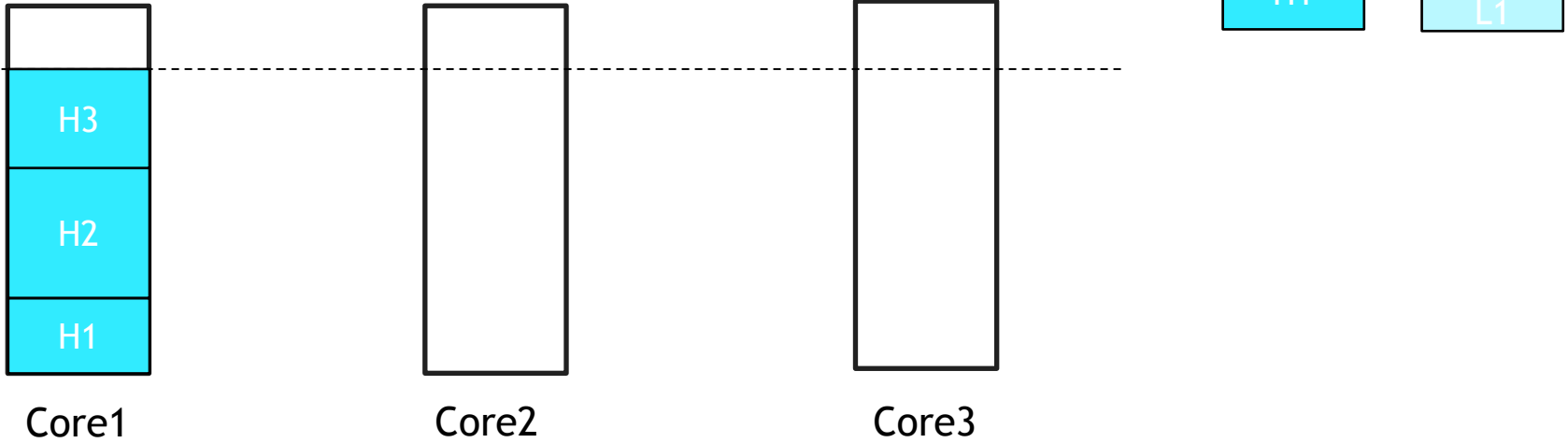
Core3



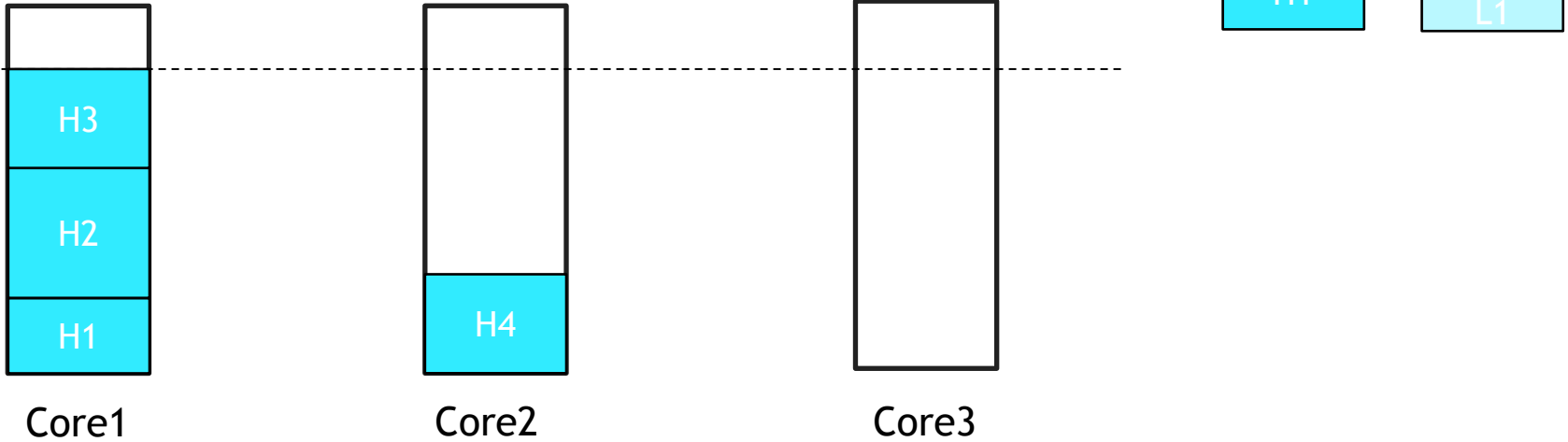
<sup>+</sup>Baruah et al. Mixed-Criticality Scheduling on Multiprocessors, RTS 14



## Method 1<sup>+</sup> (M1)

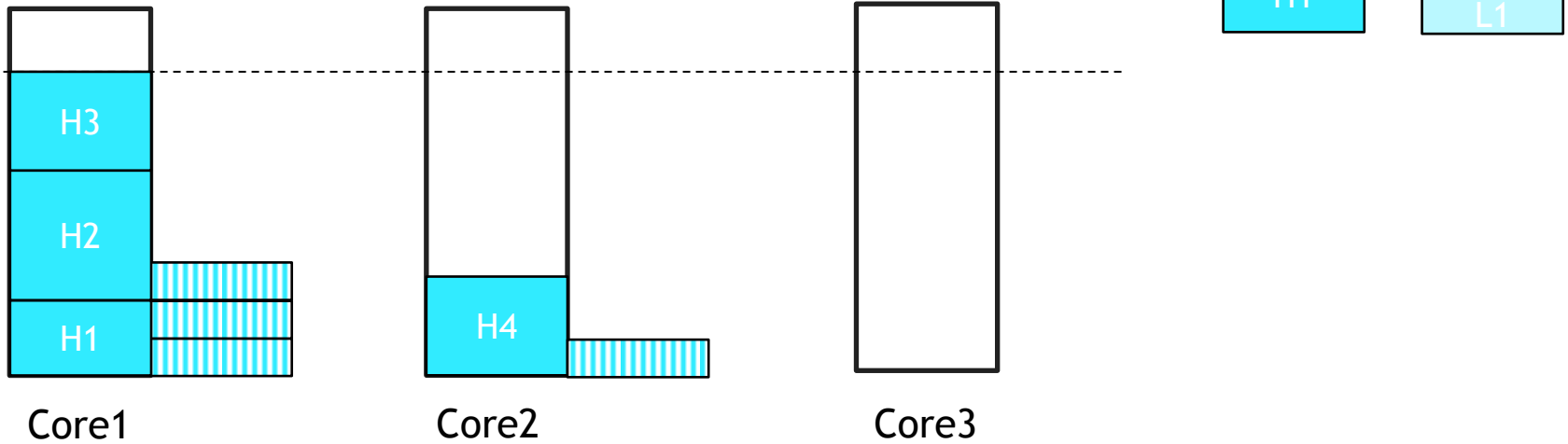


## Method 1<sup>+</sup> (M1)

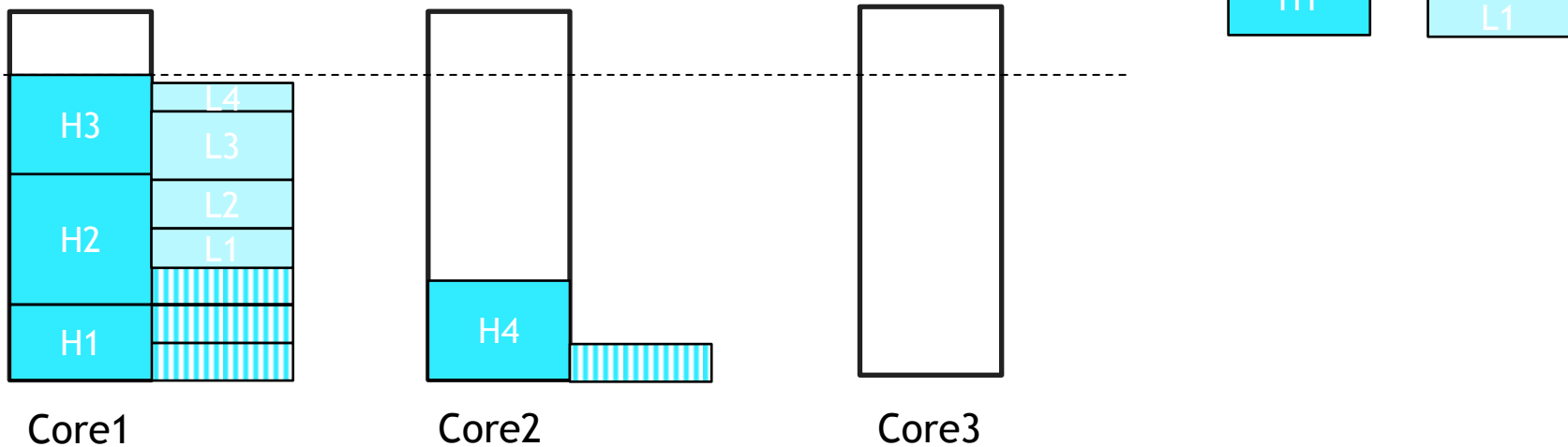


<sup>+</sup>Baruah et al. Mixed-Criticality Scheduling on Multiprocessors, RTS 14

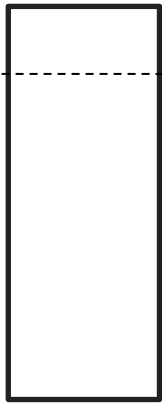
## Method 1<sup>+</sup> (M1)



## Method 1+ (M1)



## Method 2<sup>+</sup> (M2)



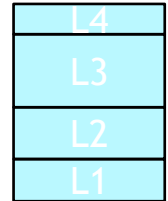
Core1



Core2



Core3



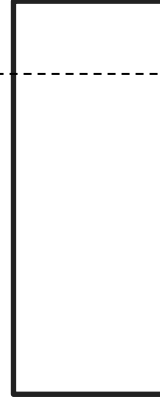
## Method 2<sup>+</sup> (M2)



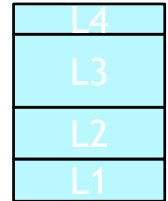
Core1



Core2



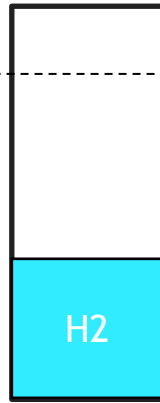
Core3



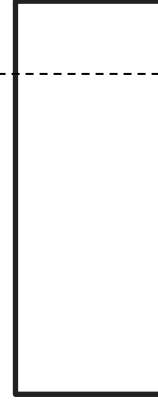
## Method 2<sup>+</sup> (M2)



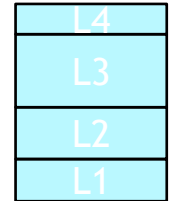
Core1



Core2



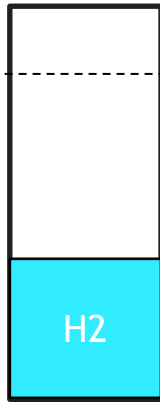
Core3



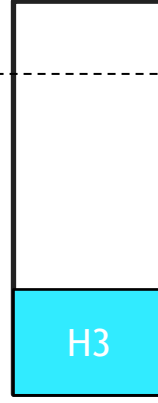
## Method 2<sup>+</sup> (M2)



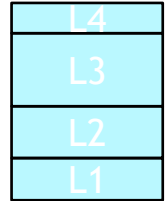
Core1



Core2

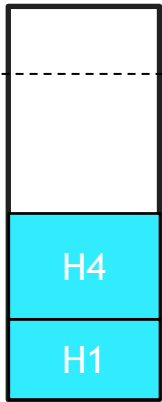


Core3

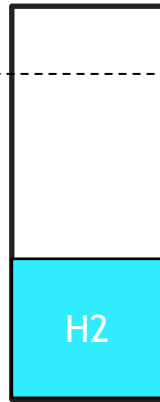




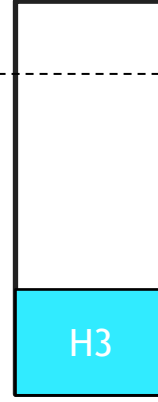
## Method 2<sup>+</sup> (M2)



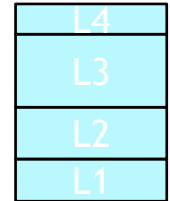
Core1



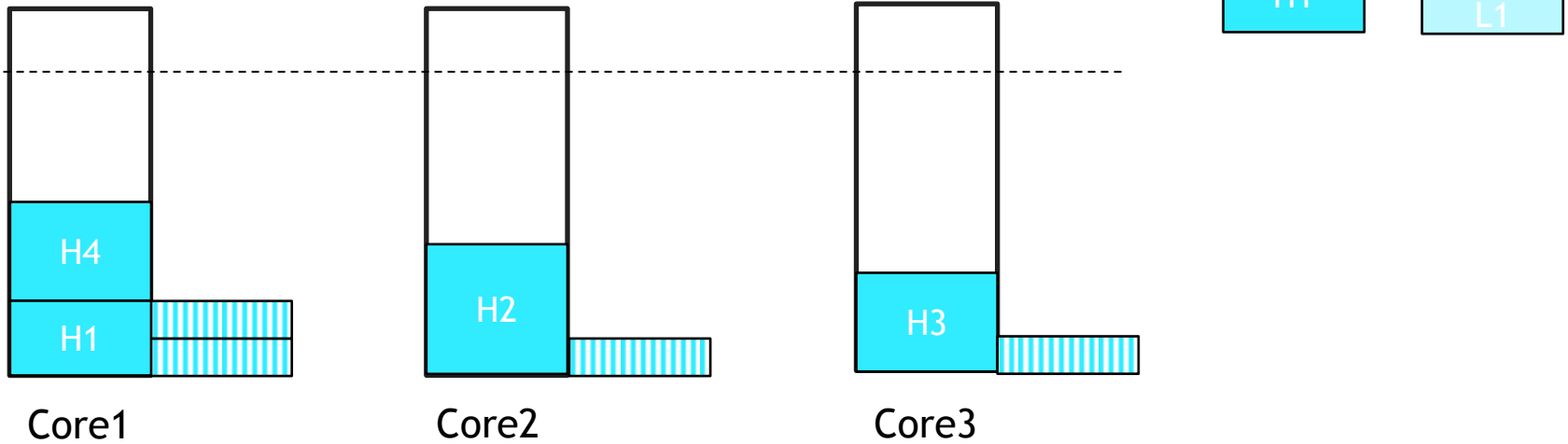
Core2



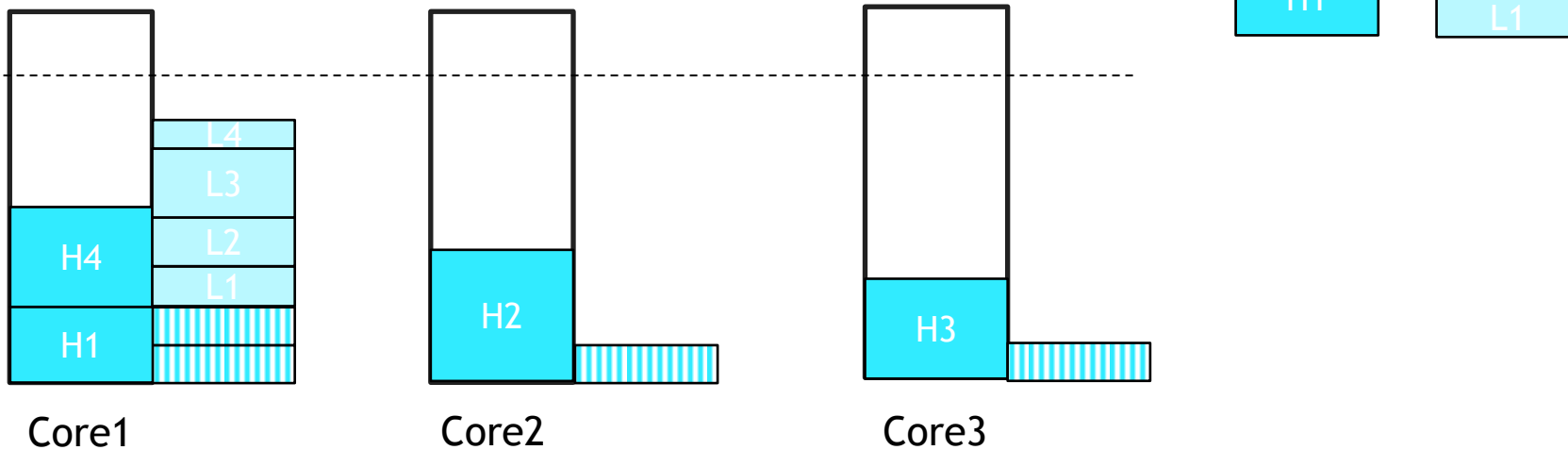
Core3



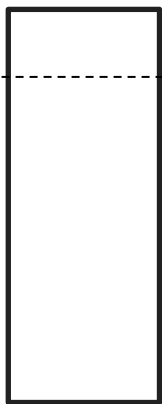
## Method 2<sup>+</sup> (M2)



## Method 2<sup>+</sup> (M2)



A new method (M3)



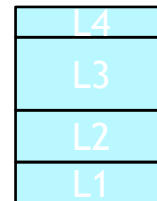
Core1



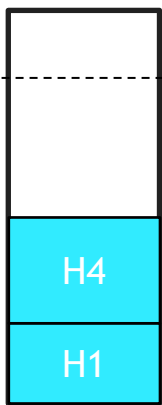
Core2



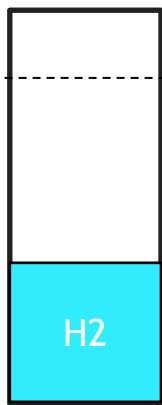
Core3



A new method (M3)



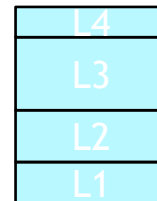
Core1



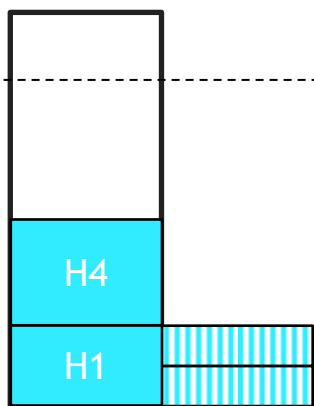
Core2



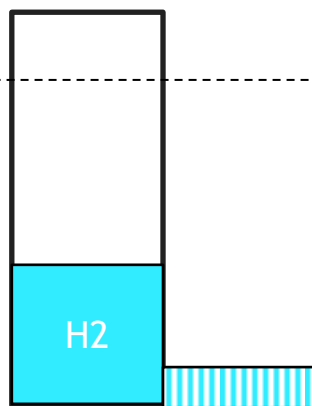
Core3



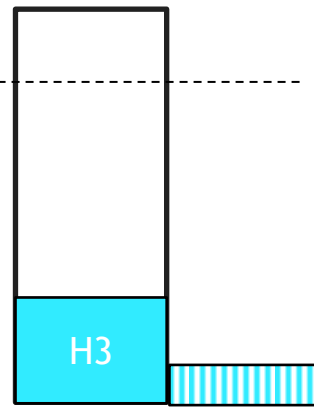
A new method (M3)



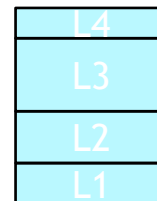
Core1



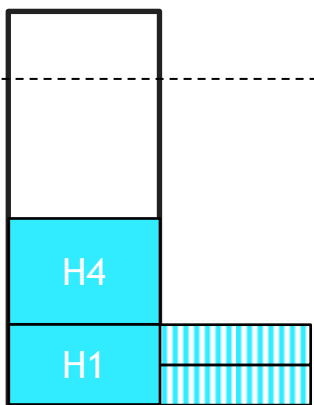
Core2



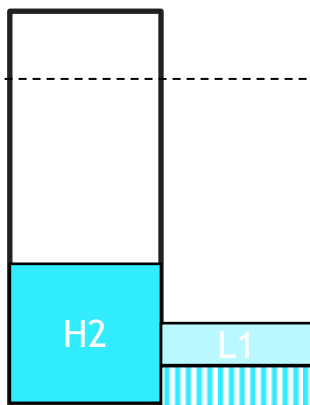
Core3



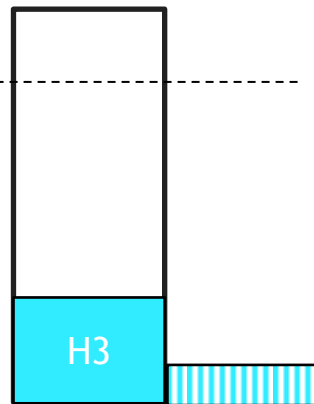
A new method (M3)



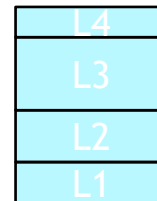
Core1



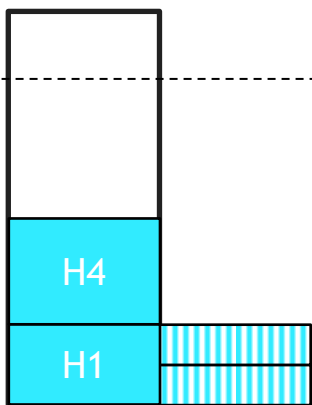
Core2



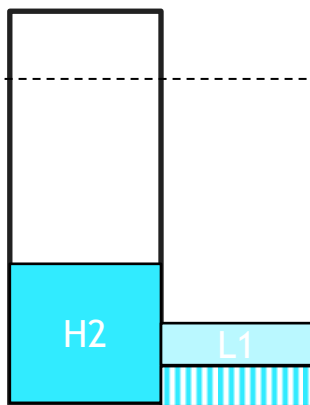
Core3



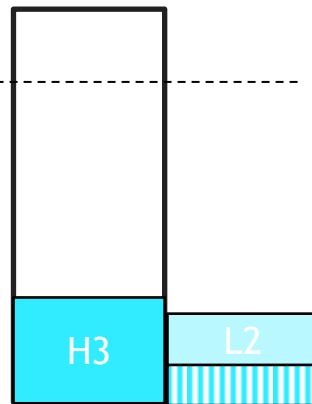
A new method (M3)



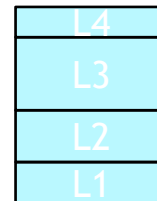
Core1



Core2

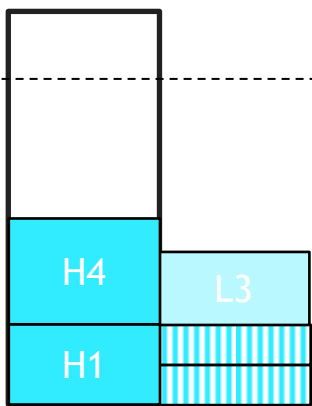


Core3

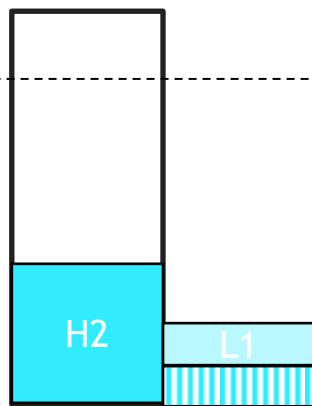




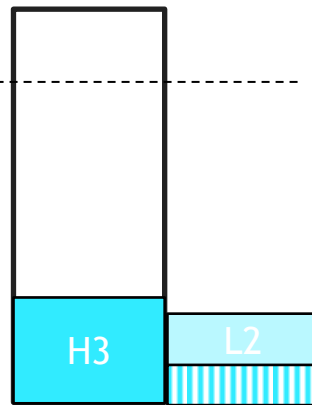
A new method (M3)



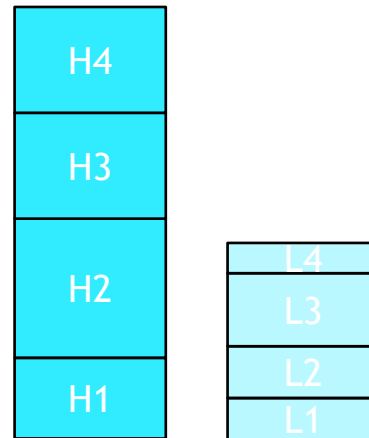
Core1



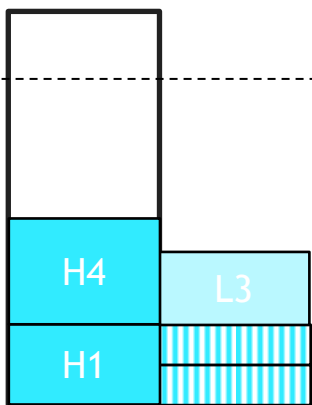
Core2



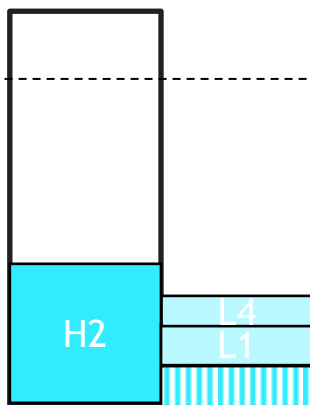
Core3



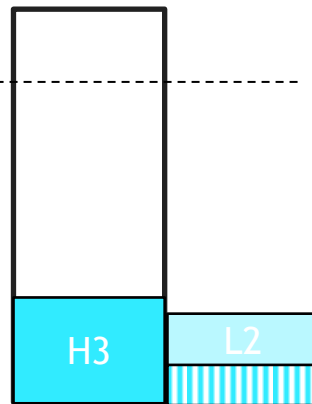
A new method (M3)



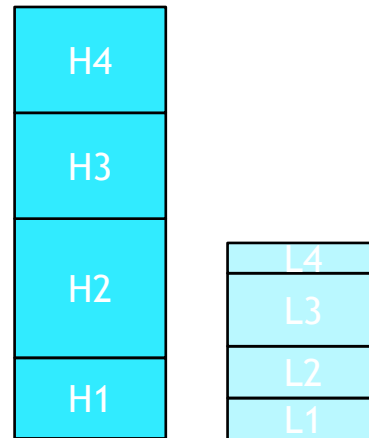
Core1



Core2



Core3



Is that all?

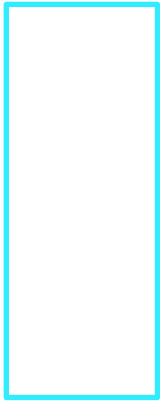
MC scheduling → mix tasks to reduce # cores

Is that all?

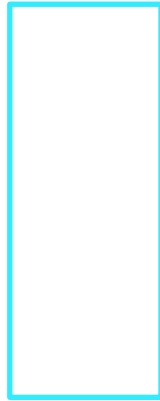
MC scheduling → mix tasks to reduce # cores

If we are conserving energy, would mixing still be good?

A different method (M4)



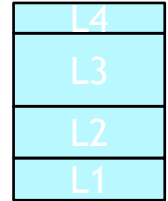
Core1



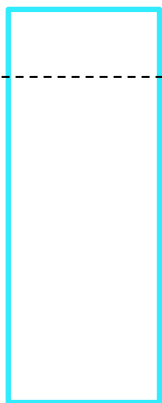
Core2



Core3



A different method (M4)



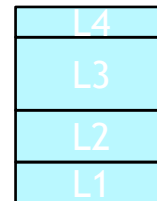
Core1



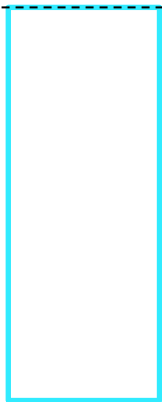
Core2



Core3



A different method (M4)



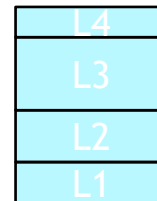
Core1



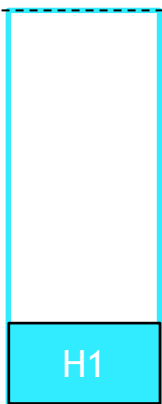
Core2



Core3



A different method (M4)



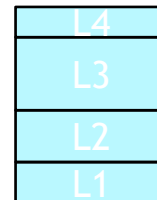
Core1



Core2

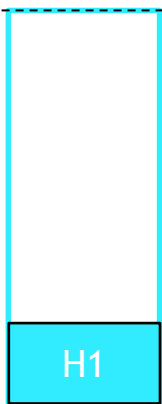


Core3

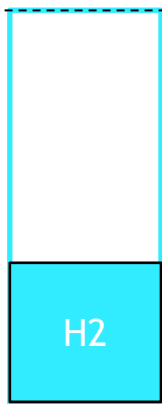




A different method (M4)



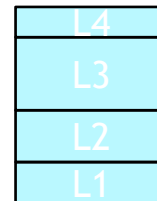
Core1



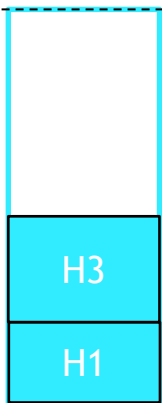
Core2



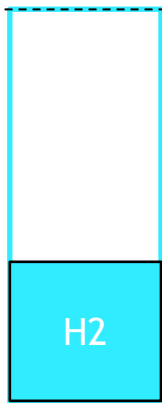
Core3



A different method (M4)



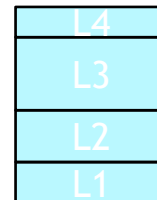
Core1



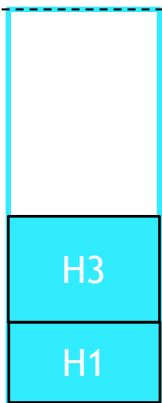
Core2



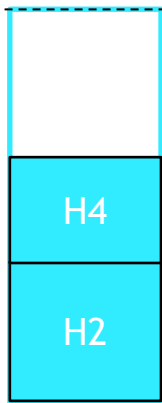
Core3



A different method (M4)



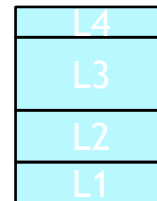
Core1



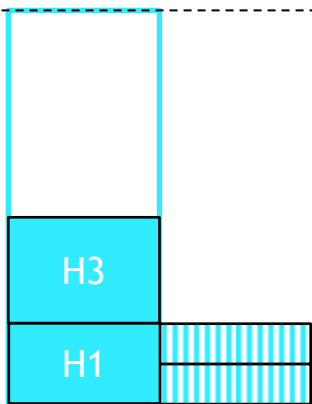
Core2



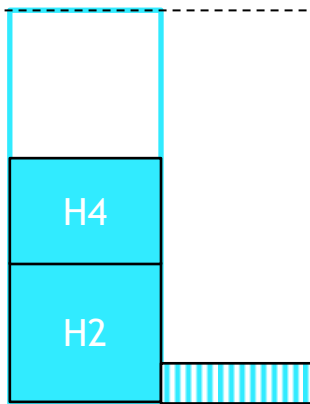
Core3



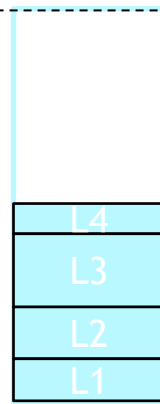
## A different method (M4)



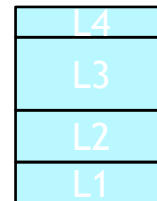
Core1



Core2



Core3



How good are the proposed solutions?

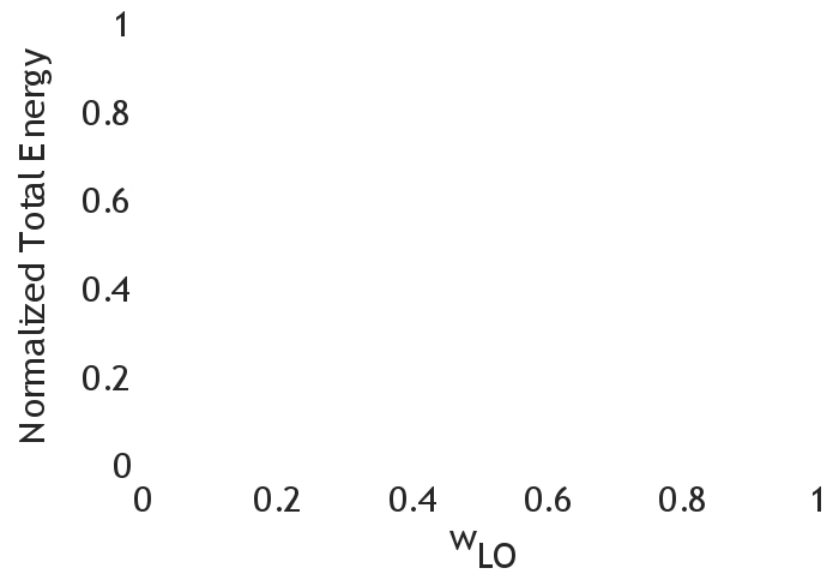
Flight management system - 7 HI, 4 LO

$$\alpha = 2, \beta = \frac{1.76W}{GHz^\alpha}, f_{min}/f_b/f_{max} = 0.5/0.8/1 GHz, P_s = 0.8W$$

Random simulations - 1000 task-sets per utilization

$$\alpha = 2, \beta = \frac{1.76W}{GHz^\alpha}, f_{min}/f_b/f_{max} = 0.5/0.8/1 GHz, P_s = 0.5W$$

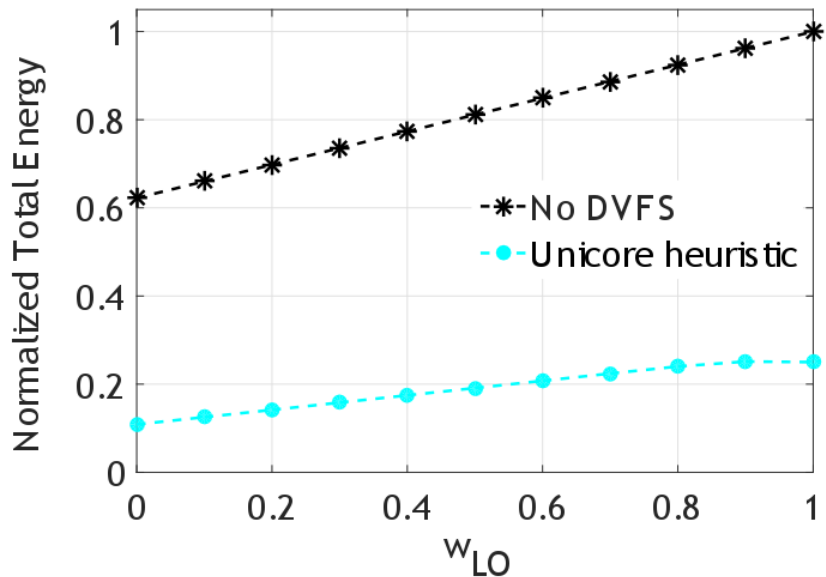
FMS



FMS

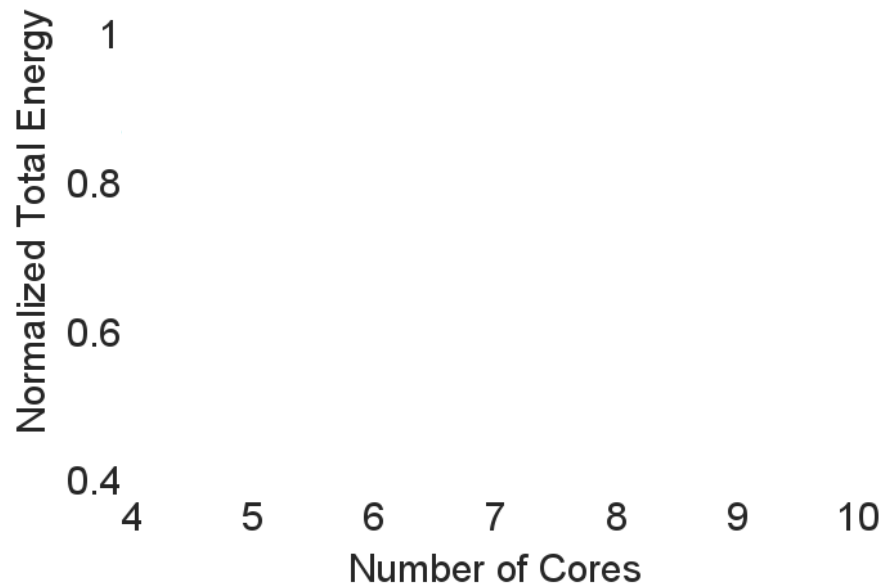
30%~50% energy reduction

Contribution factor does impact!



## Random simulations

$$U = 3, w_{LO} = w_{HI} = 0.5$$





## Random simulations

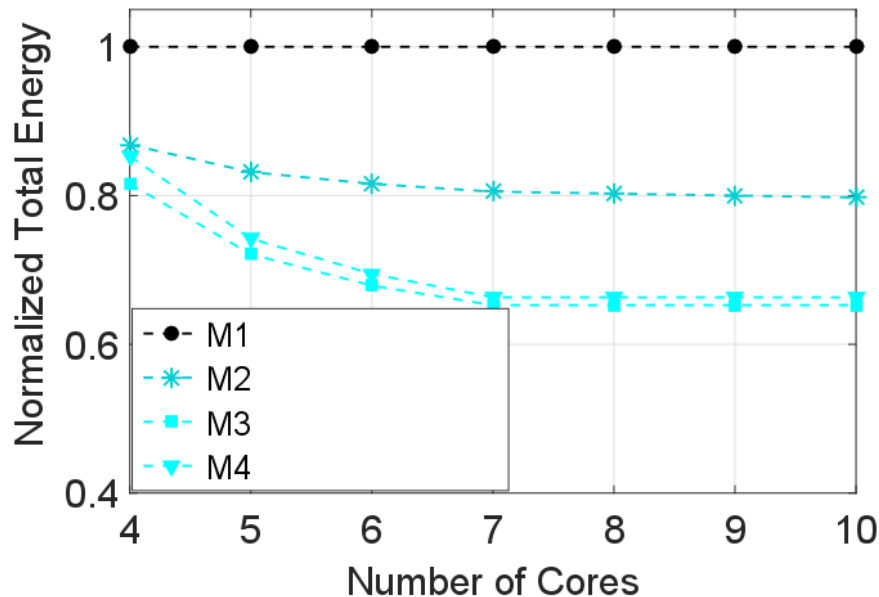
$$U = 3, w_{LO} = w_{HI} = 0.5$$

## Proposed methods perform well

7cores: ~30% (~20%) more saving than M1 (M2)

## Isolation pays-off!

*very close to M3*





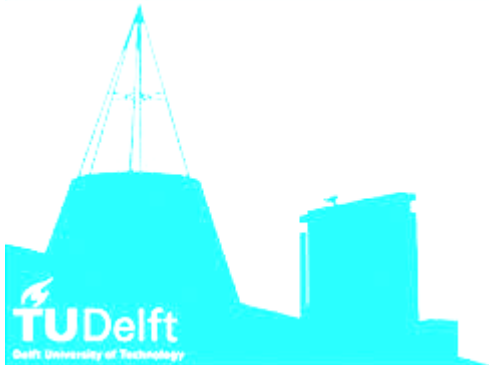
Pengcheng Huang  
Georgia Giannopoulou  
Lothar Thiele

Minimize static & dynamic energy.

Optimal & fast numerical solutions for uncore.

Energy-aware mappings for multicore.

If energy is a concern, isolate!



Sujay Narayana  
R. Venkatesha Prasad



Pengcheng Huang  
Georgia Giannopoulou  
Lothar Thiele



Sujay Narayana  
R. Venkatesha Prasad

